

# Three-nucleon forces at neutron-rich extremes

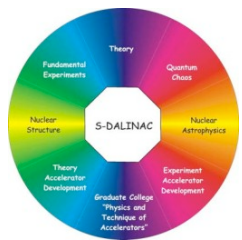
Achim Schwenk



TECHNISCHE  
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**George Bertsch Fest**  
Seattle, Sept. 8, 2012



**DFG**



*Minerva  
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**ARCHES**

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Bundesministerium  
für Bildung  
und Forschung



# Outline

Understanding three-nucleon (3N) forces

3N forces and neutron-rich nuclei

with **J.D. Holt, J. Menendez, T. Otsuka, T. Suzuki**

3N forces and neutron matter/stars

with **K. Hebeler, T. Krüger, I. Tews,**  
**J.M. Lattimer, C.J. Pethick**

Electroweak interactions and 3N forces

with **J. Menendez, D. Gazit**



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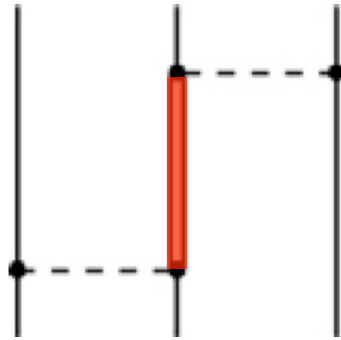




# Why are there three-nucleon (3N) forces?

Nucleons are finite-mass composite particles,  
can be excited to resonances

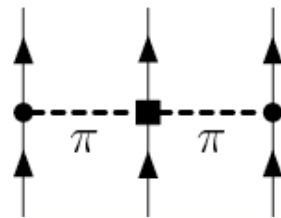
dominant contribution from  $\Delta(1232 \text{ MeV})$



+ many shorter-range parts

chiral effective field theory (EFT)

Delta-less ( $\Delta$  is treated as heavy):



+ shorter-range parts

EFT provides a systematic and powerful approach for 3N forces



# Chiral Effective Field Theory for nuclear forces

Separation of scales: low momenta  $\frac{1}{\lambda} = Q \ll \Lambda_b$  breakdown scale  $\sim 500$  MeV

	NN	3N	4N
LO $\mathcal{O}\left(\frac{Q^0}{\Lambda^0}\right)$			
NLO $\mathcal{O}\left(\frac{Q^2}{\Lambda^2}\right)$			
N <sup>2</sup> LO $\mathcal{O}\left(\frac{Q^3}{\Lambda^3}\right)$			
N <sup>3</sup> LO $\mathcal{O}\left(\frac{Q^4}{\Lambda^4}\right)$			

include long-range pion physics

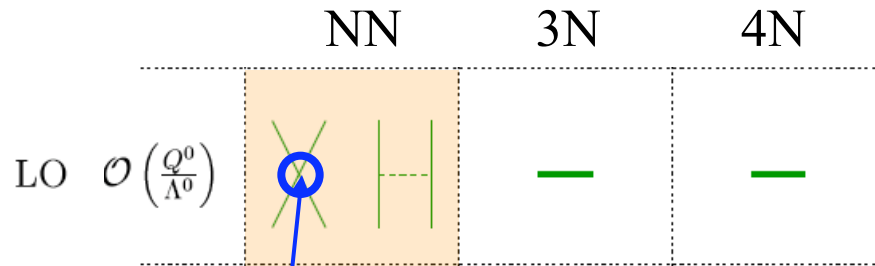
few short-range couplings,  
fit to experiment once

systematic: can work to desired  
accuracy and obtain **error estimates**

expansion parameter  $\sim 1/3$

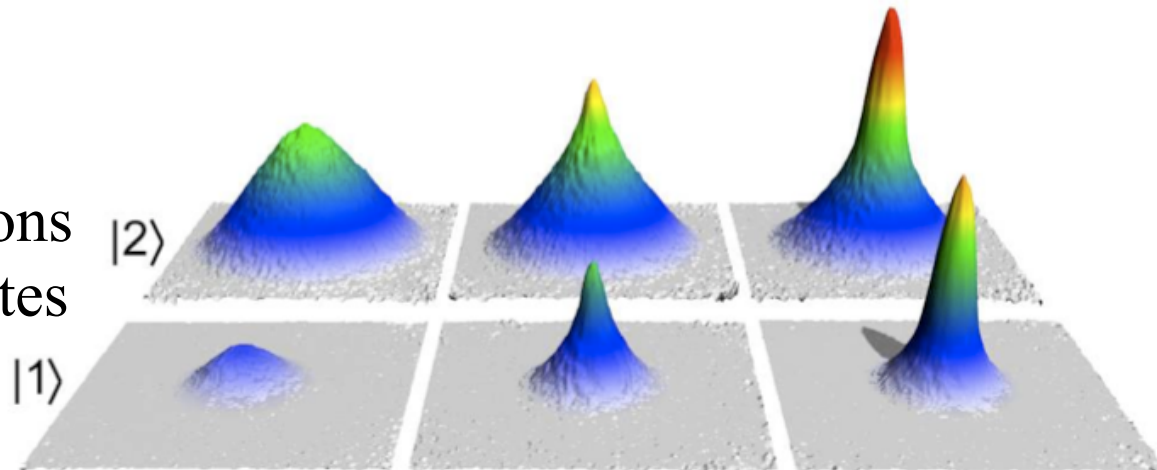
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large scattering length physics – **The Bertsch problem**

${}^6\text{Li}$  fermions  
2 spin states

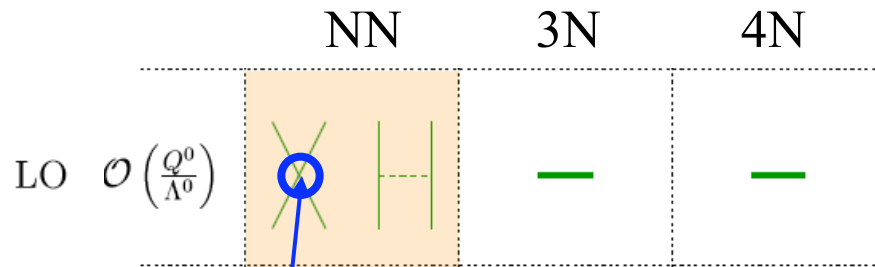


from M. Zwierlein

neutrons with same density, temperature and spin polarization  
have the same properties!

# Chiral Effective Field Theory for nuclear forces

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large scattering length physics – **The Bertsch problem**

As  $T \rightarrow 0$ , the Fermi energy  $E_F$  is the only intensive energy scale, so the chemical potential must be related to  $E_F$  by a universal number,  $\mu = \xi E_F$ , where  $\xi$  is known as the Bertsch parameter



**Revealing the Superfluid Lambda Transition in the Universal Thermodynamics of a Unitary Fermi Gas**

Mark J. H. Ku, *et al.*

*Science* **335**, 563 (2012);

DOI: 10.1126/science.1214987



# Chiral Effective Field Theory and many-body forces

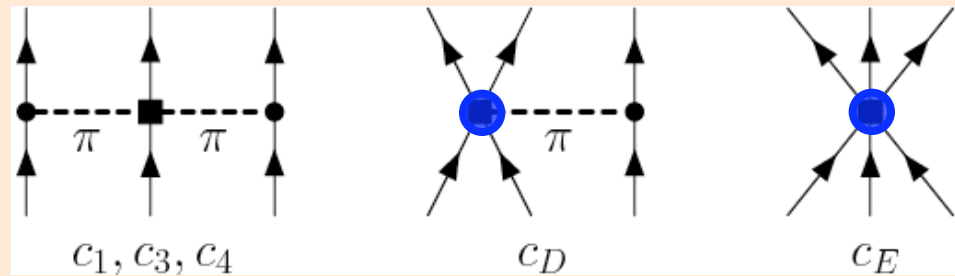
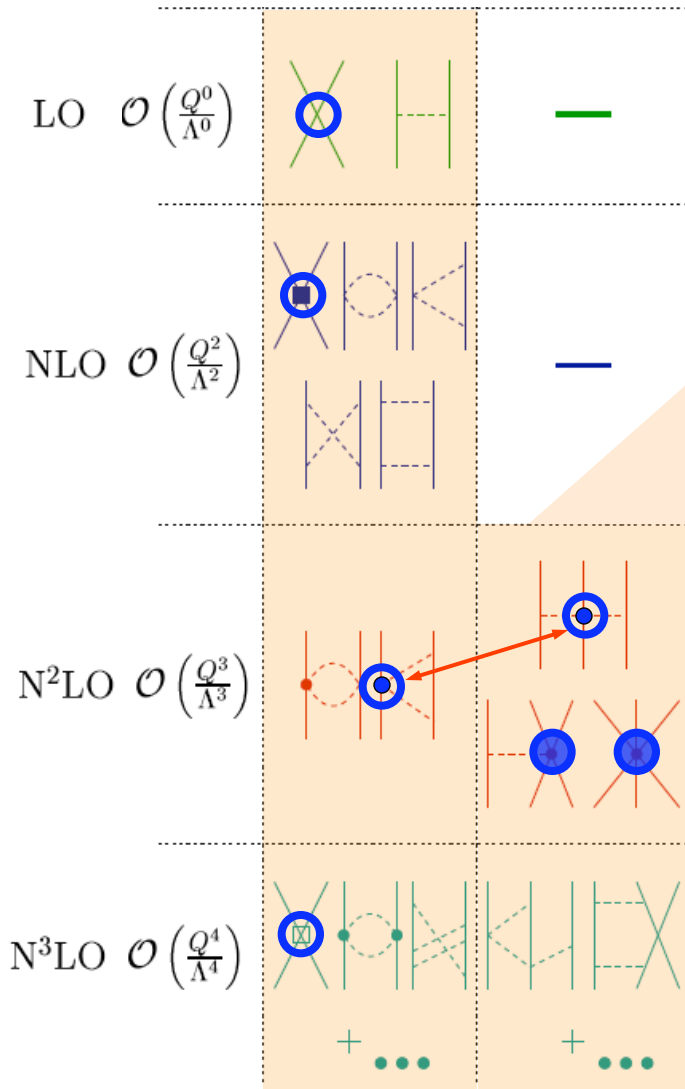
Separation of scales: low momenta  $\frac{1}{\Lambda} = Q \ll \Lambda_b$  breakdown scale  $\sim 500$  MeV

NN

3N

consistent NN-3N interactions

3N,4N: only 2 new couplings to N<sup>3</sup>LO



$c_i$  from  $\pi$ N and NN Meissner et al. (2007)

$$c_1 = -0.9^{+0.2}_{-0.5}, \quad c_3 = -4.7^{+1.2}_{-1.0}, \quad c_4 = 3.5^{+0.5}_{-0.2}$$

single- $\Delta$ :  $c_1=0$ ,  $c_3=-c_4/2=-3 \text{ GeV}^{-1}$

$c_D, c_E$  fit to  ${}^3\text{H}$  binding energy and  ${}^4\text{He}$  radius (or  ${}^3\text{H}$  beta decay)

# Subleading chiral 3N forces

parameter-free N<sup>3</sup>LO Bernard et al. (2007,2011), Ishikawa, Robilotta (2007)

one-loop contributions:

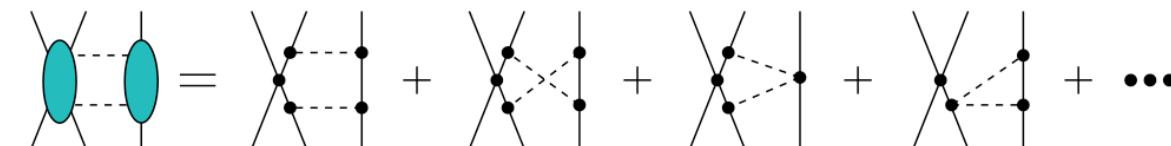
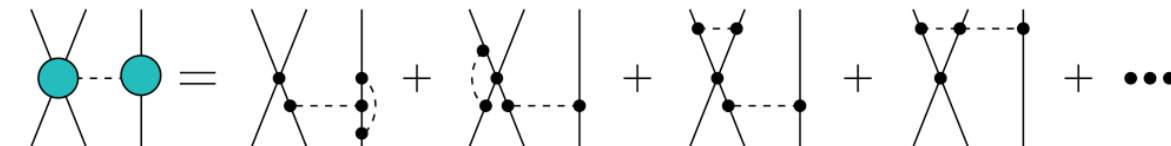
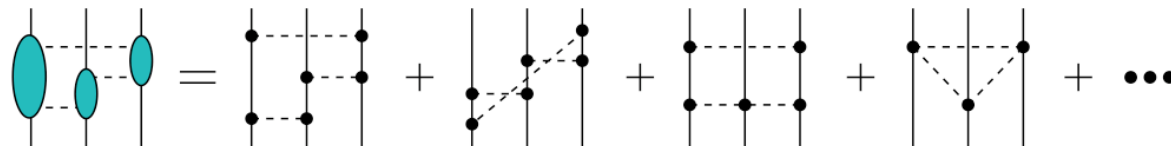
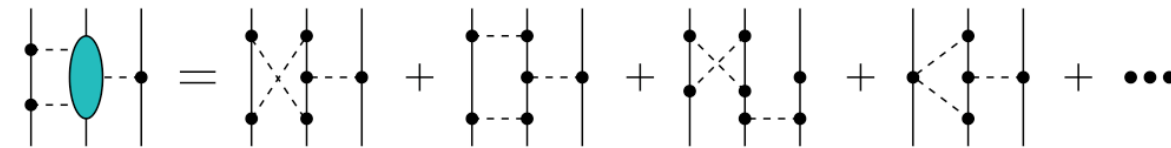
2 $\pi$ -exchange, 2 $\pi$ -1 $\pi$ -exchange, rings, contact-1 $\pi$ -, contact-2 $\pi$ -exchange



decrease  $c_i$  strengths

$$\delta c_3 = -\delta c_4 = 1 \text{ GeV}^{-1}$$

comparable to  
N<sup>2</sup>LO uncertainty



1/m corrections: spin-orbit parts, interesting for  $A_y$  puzzle

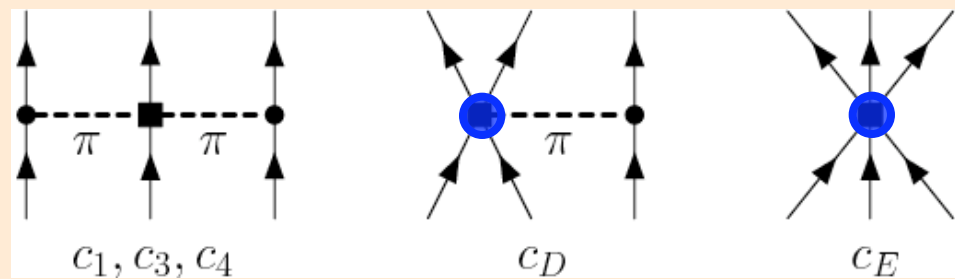
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$c_D$ ,  $c_E$  don't contribute for **neutrons** because of Pauli principle and pion coupling to spin, also for  $c_4$

Hebeler, AS (2010)



all 3- and 4-neutron forces are predicted to N<sup>3</sup>LO!



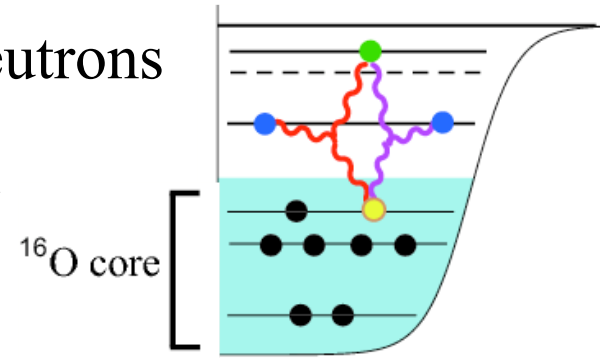
# The shell model - impact of 3N forces

include ‘normal-ordered’ 2-body part of 3N forces (enhanced by core A)

leads to repulsive interactions between valence neutrons

contributions from residual three valence-nucleon interactions suppressed by  $E_{\text{ex}}/E_{\text{F}} \sim N_{\text{valence}}/N_{\text{core}}$

Friman, AS (2011)



residual 3N amplified in most neutron-rich nuclei C. Caesar, J. Simonis et al. (2012)

# Oxygen isotopes - impact of 3N forces

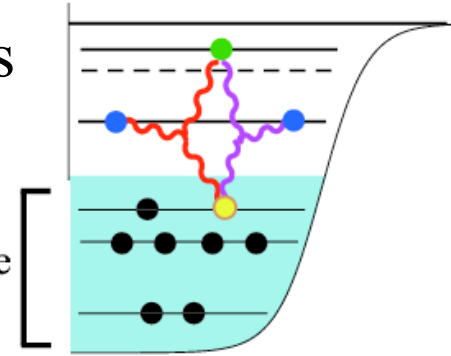
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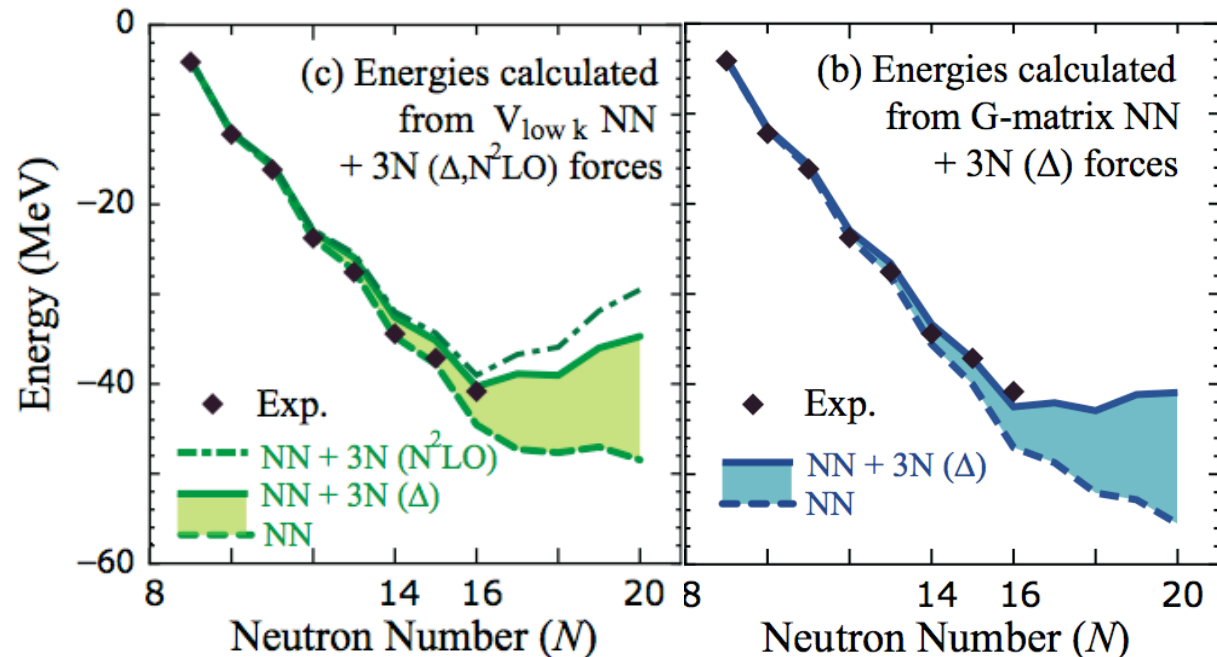
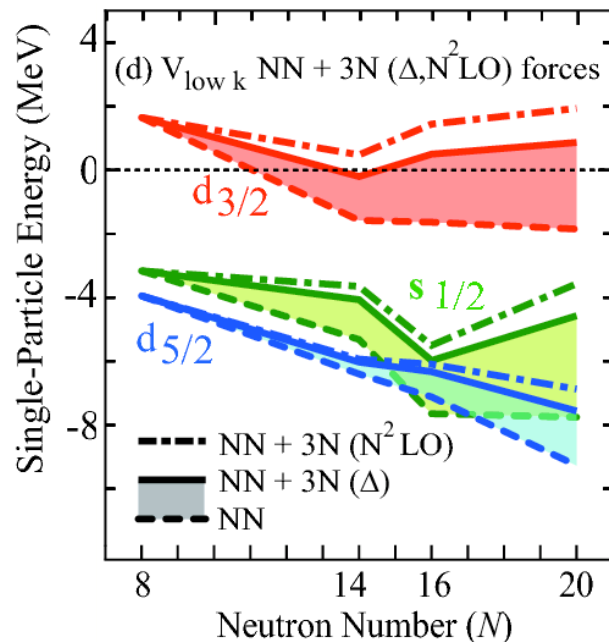
contributions from residual three valence-nucleon

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Friman, AS (2011)



$d_{3/2}$  orbital remains unbound from  $^{16}\text{O}$  to  $^{28}\text{O}$



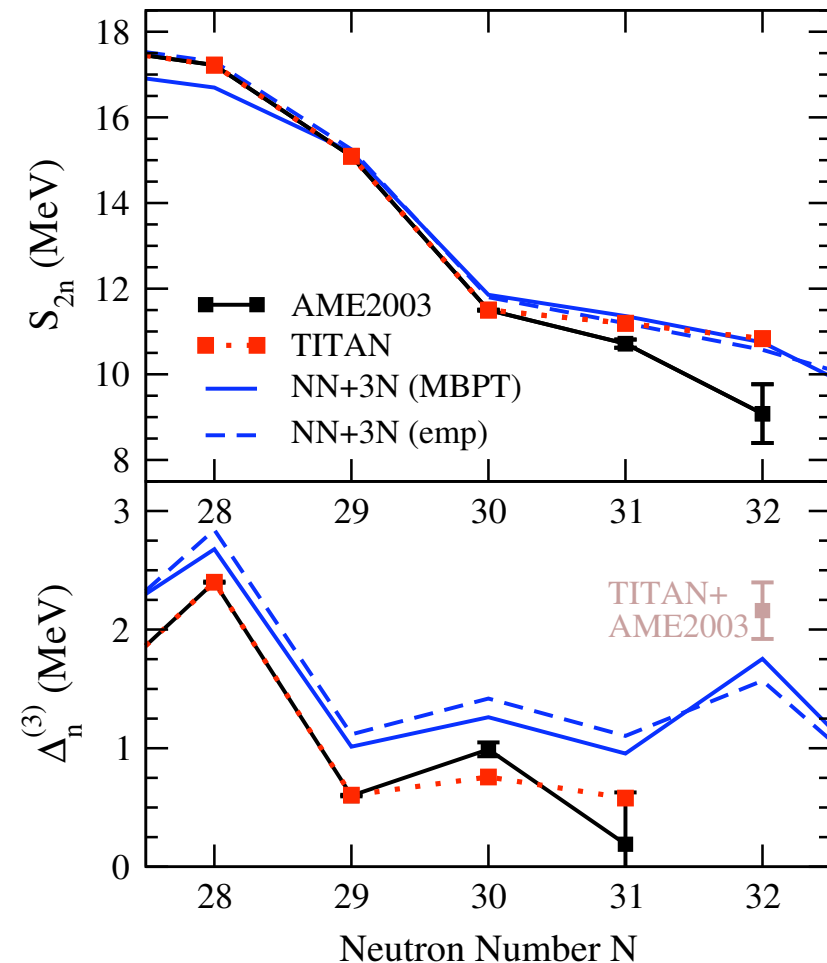
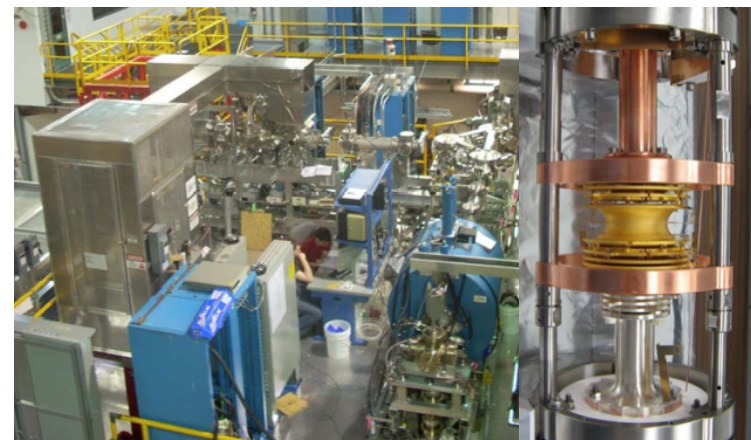
microscopic explanation of the oxygen anomaly Otsuka et al. (2010)

# new $^{51,52}\text{Ca}$ TITAN measurements

$^{52}\text{Ca}$  is 1.75 MeV more bound  
compared to atomic mass evaluation

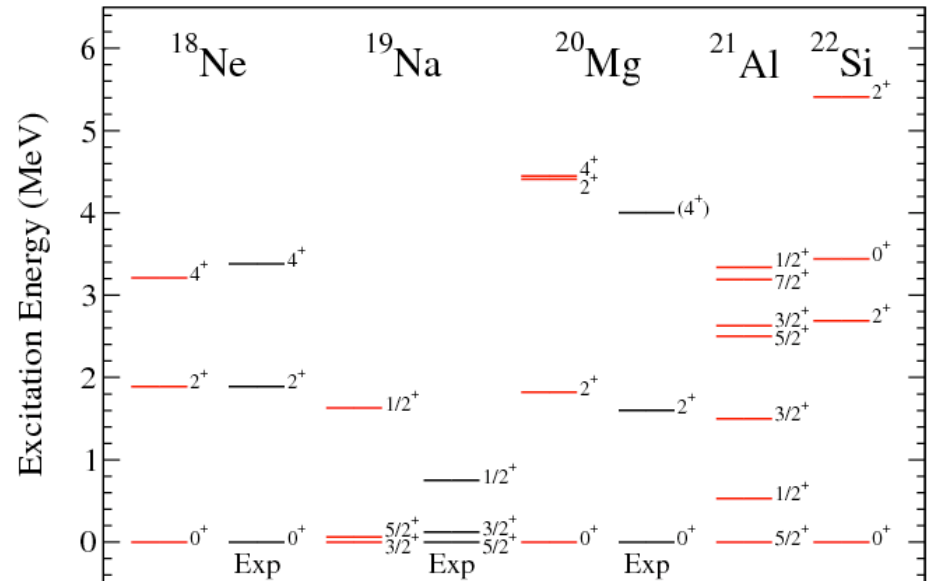
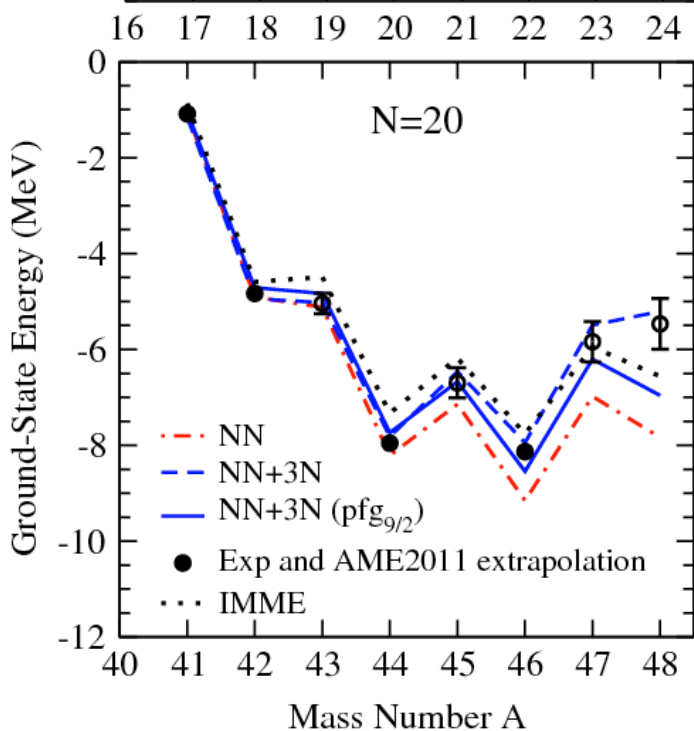
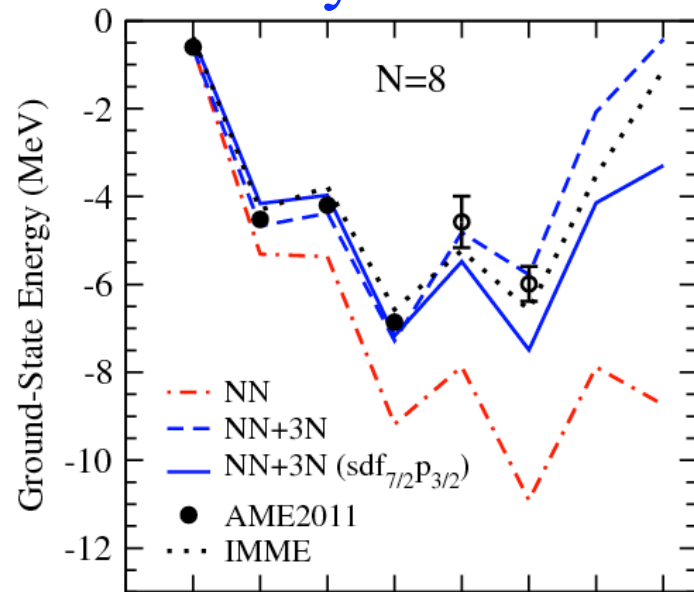
Gallant et al. (2012)

behavior of two-neutron separation  
energy  $S_{2n}$  and odd-even staggering  $\Delta_n$   
agrees with NN+3N predictions

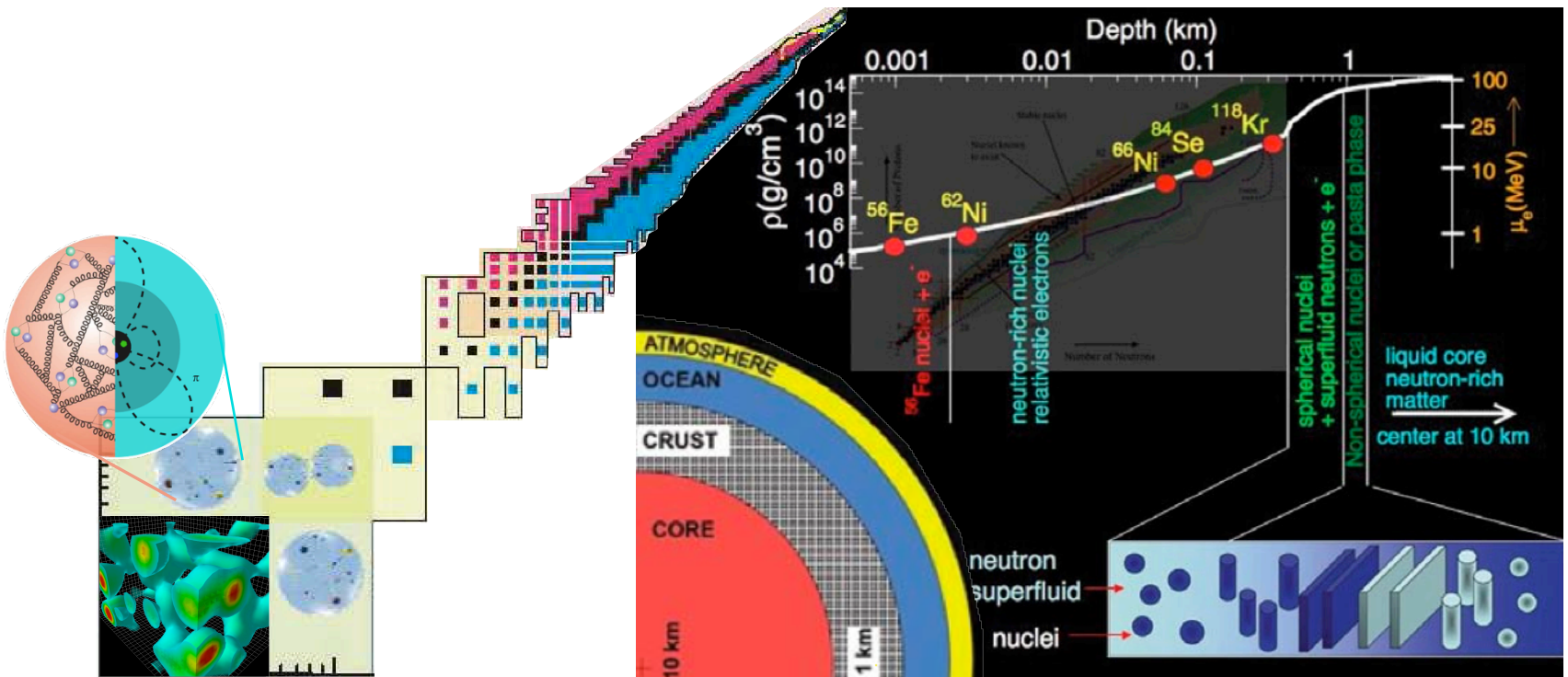




# Three-body forces and proton-rich systems Holt, Menendez, AS



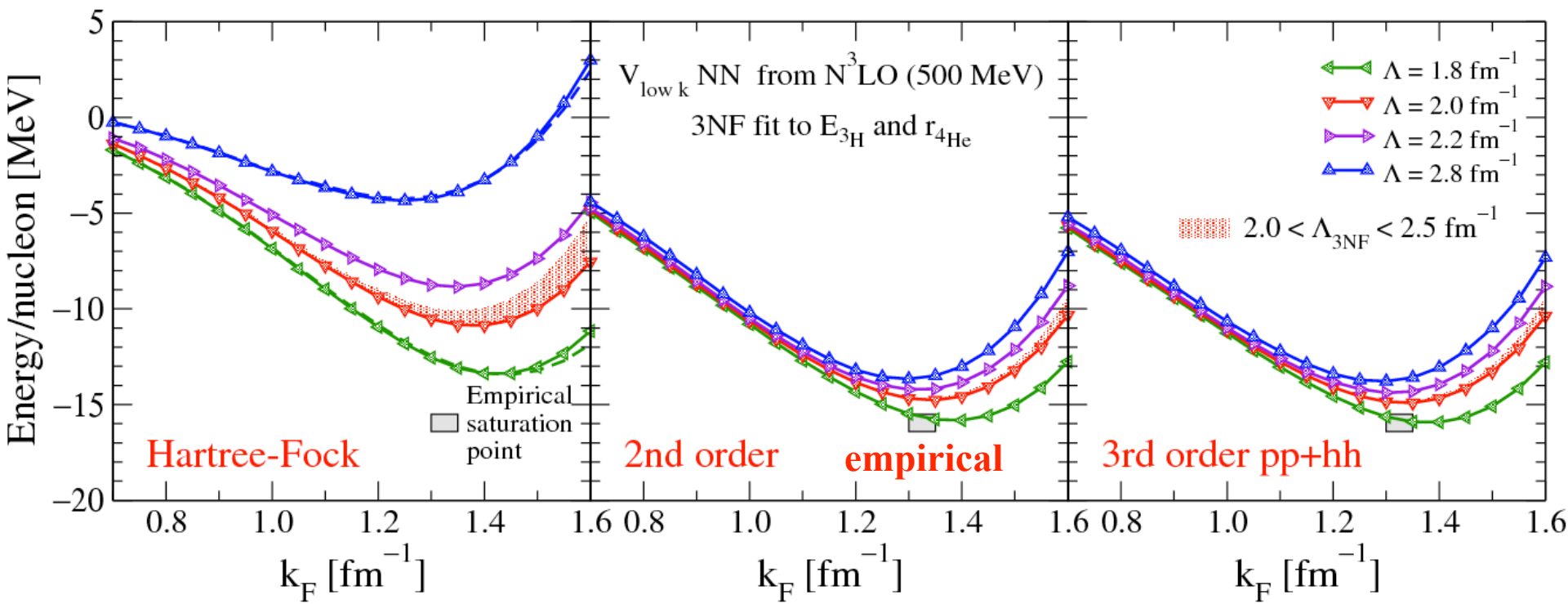
# Neutron matter and neutron stars



# Impact of 3N forces on nuclear matter

chiral 3N forces fit to light nuclei  
predict nuclear matter saturation  
with theoretical uncertainties

Hebeler et al. (2011), Bogner et al. (2005)

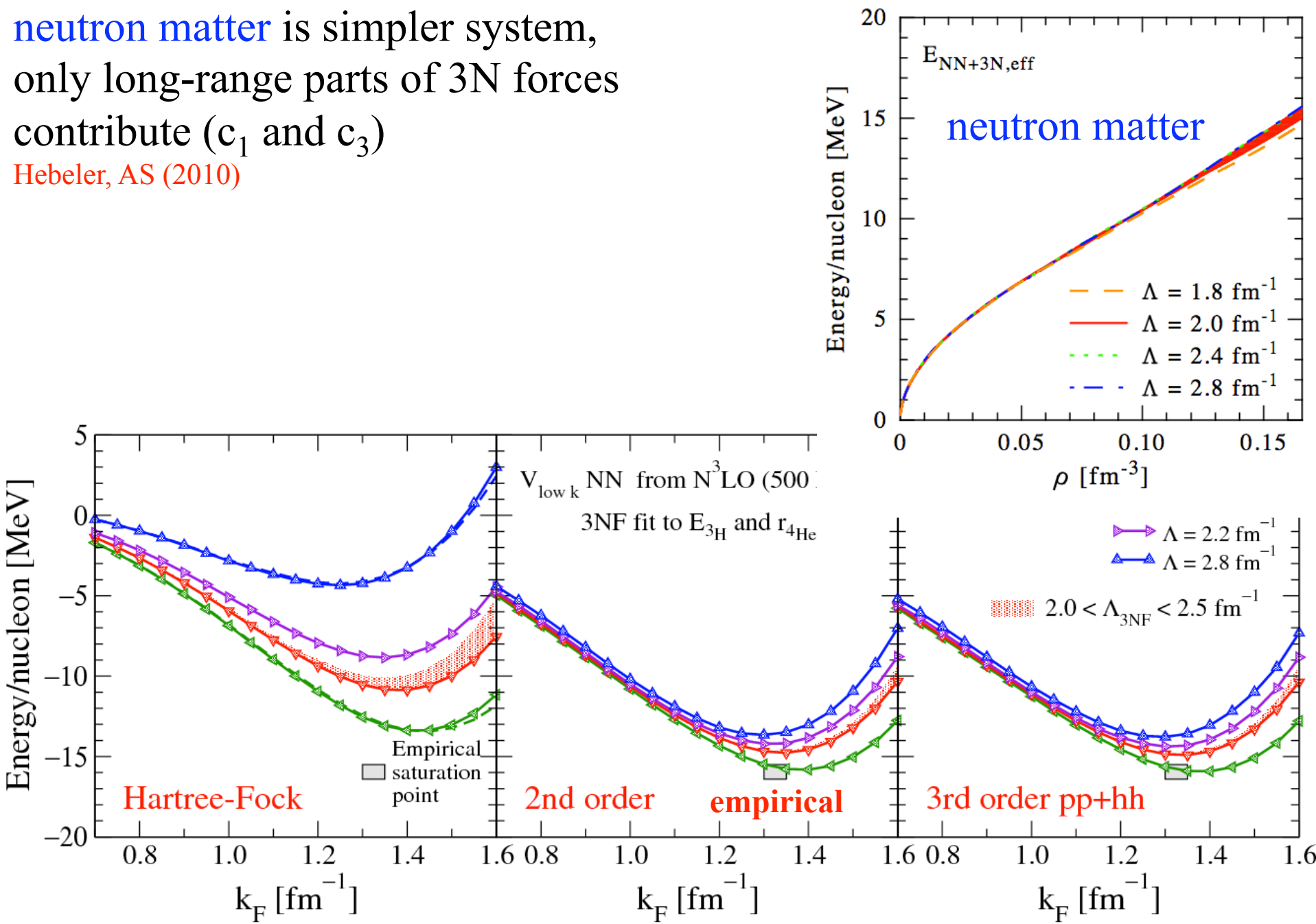




# Impact of 3N forces on neutron matter

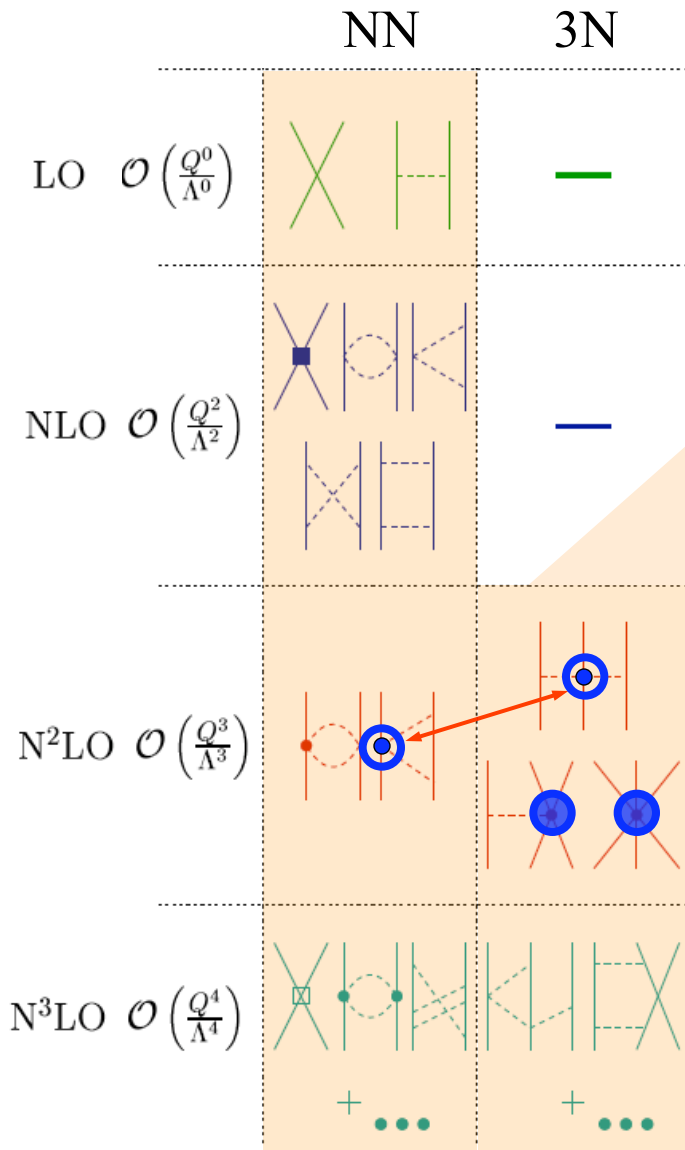
neutron matter is simpler system,  
only long-range parts of 3N forces  
contribute ( $c_1$  and  $c_3$ )

Hebeler, AS (2010)



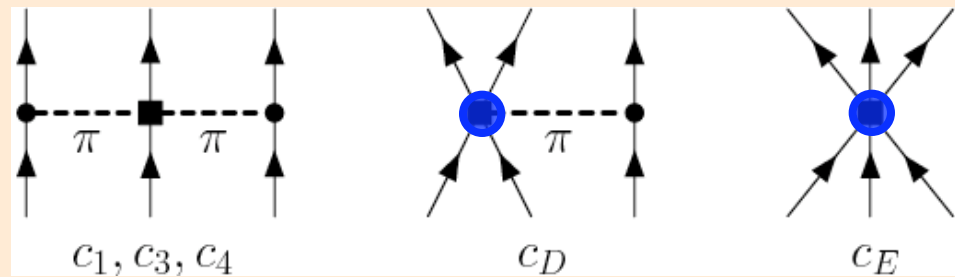
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long-range 3N:  $c_i$  from  $\pi$ N and NN

$$c_1 = -0.9^{+0.2}_{-0.5}, \quad c_3 = -4.7^{+1.2}_{-1.0}, \quad c_4 = 3.5^{+0.5}_{-0.2}$$

3- and 4-neutron forces are predicted to N<sup>3</sup>LO ( $c_{D,E}$  don't contribute)

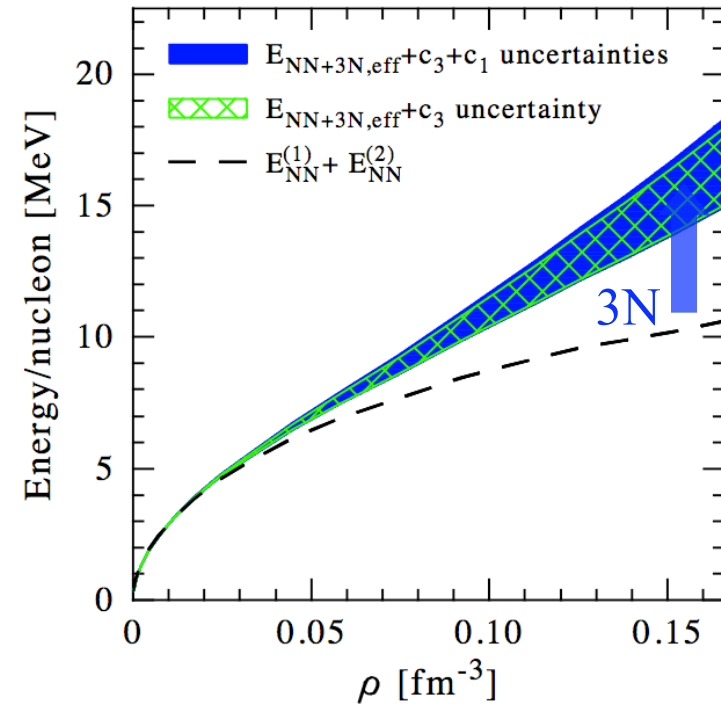
Hebeler, AS (2010)

# Impact of 3N forces on neutron matter

neutron matter uncertainties

dominated by 3N forces ( $c_3$  coupling)

Hebeler, AS (2010)

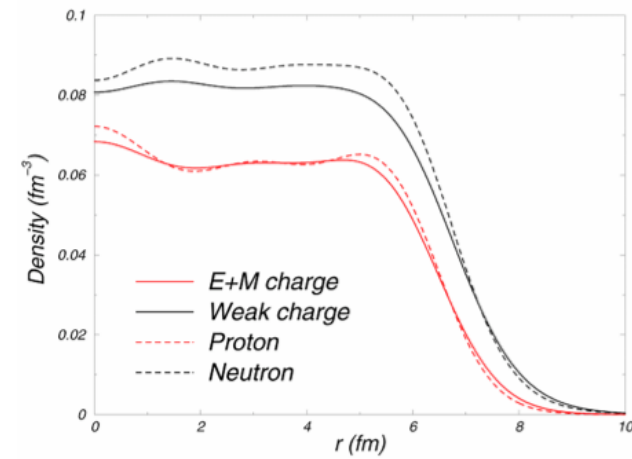


# Neutron skin of $^{208}\text{Pb}$

probes neutron matter energy/pressure,  
neutron matter band predicts

neutron skin of  $^{208}\text{Pb}$ :  $0.17 \pm 0.03$  fm

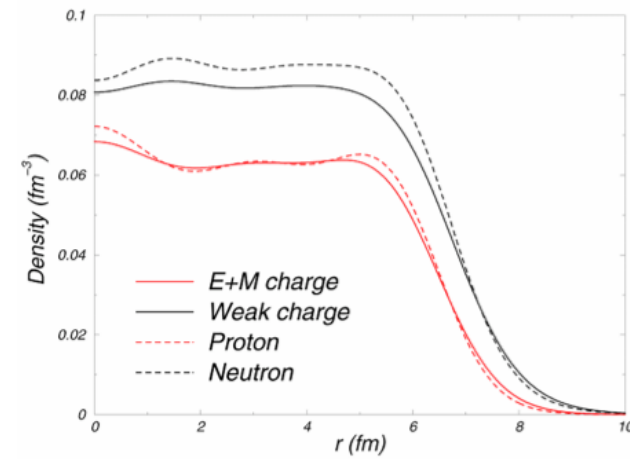
Hebeler et al. (2010)



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Hebeler et al. (2010)



in excellent agreement with extraction from complete E1 response  
 $0.156^{+0.025}_{-0.021}$  fm

PRL 107, 062502 (2011)

PHYSICAL REVIEW LETTERS

week ending  
5 AUGUST 2011

## Complete Electric Dipole Response and the Neutron Skin in $^{208}\text{Pb}$

A benchmark experiment on  $^{208}\text{Pb}$  shows that polarized proton inelastic scattering at very forward angles including  $0^\circ$  is a powerful tool for high-resolution studies of electric dipole ( $E1$ ) and spin magnetic dipole ( $M1$ ) modes in nuclei over a broad excitation energy range to test up-to-date nuclear models. The extracted  $E1$  polarizability leads to a neutron skin thickness  $r_{\text{skin}} = 0.156^{+0.025}_{-0.021}$  fm in  $^{208}\text{Pb}$  derived within

PREX: neutron skin from parity-violating electron-scattering at JLAB  
electron exchanges Z-boson, couples preferentially to neutrons  
goal II:  $\pm 0.06$  fm

PRL 108, 112502 (2012)

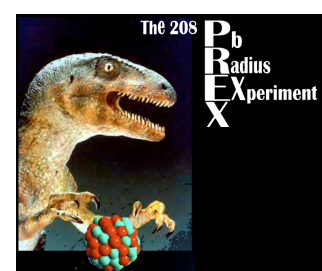
PHYSICAL REVIEW LETTERS

week ending  
16 MARCH 2012



## Measurement of the Neutron Radius of $^{208}\text{Pb}$ through Parity Violation in Electron Scattering

We report the first measurement of the parity-violating asymmetry  $A_{\text{PV}}$  in the elastic scattering of polarized electrons from  $^{208}\text{Pb}$ .  $A_{\text{PV}}$  is sensitive to the radius of the neutron distribution ( $R_n$ ). The result  $A_{\text{PV}} = 0.656 \pm 0.060(\text{stat}) \pm 0.014(\text{syst})$  ppm corresponds to a difference between the radii of the neutron and proton distributions  $R_n - R_p = 0.33^{+0.16}_{-0.18}$  fm and provides the first electroweak observation of the neutron skin which is expected in a heavy, neutron-rich nucleus.



# Symmetry energy and pressure of neutron matter

neutron matter band predicts  
symmetry energy  $S_v$  and  
its density dependence  $L$

comparison to experimental  
and observational constraints

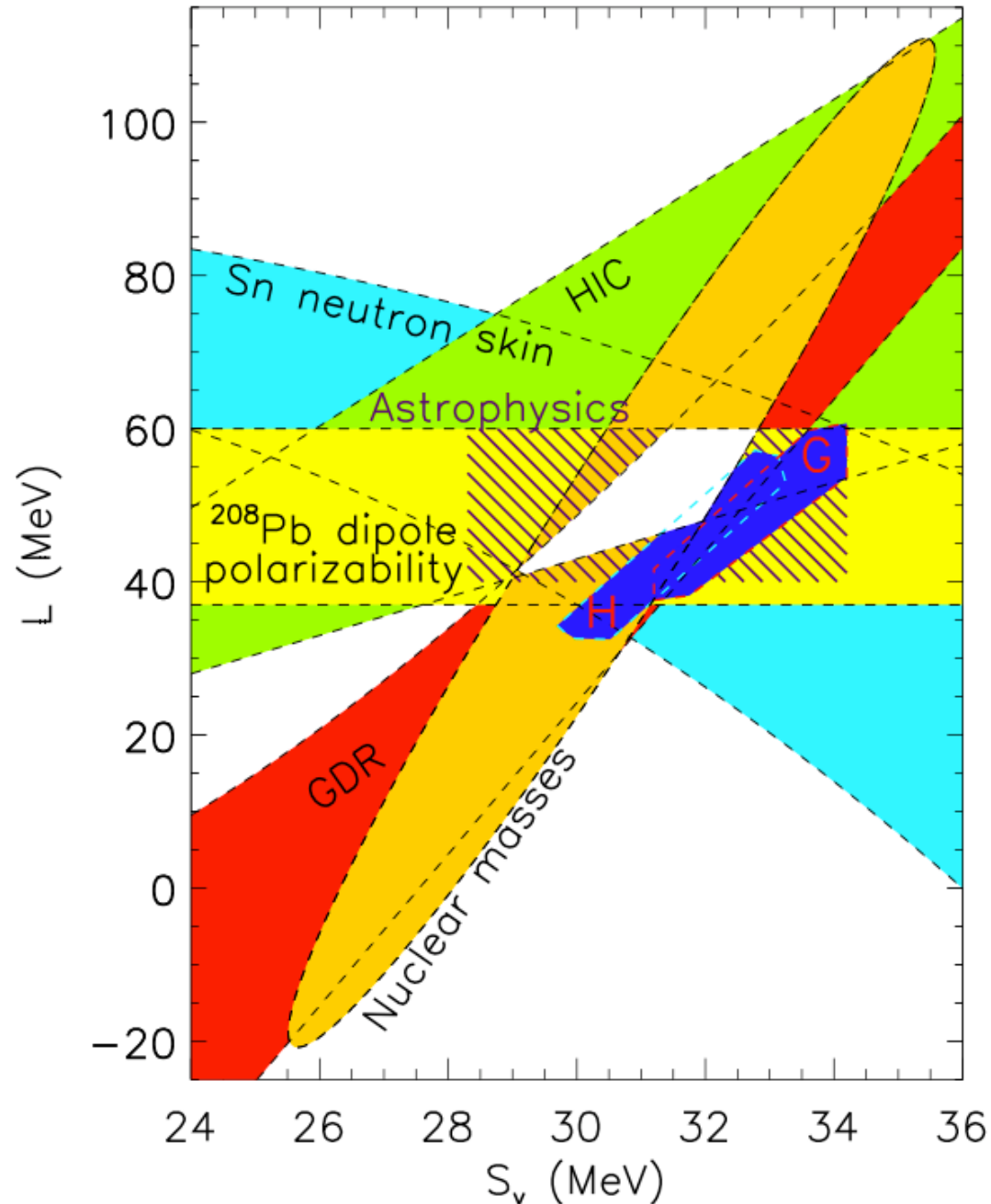
Lattimer, Lim (2012)

neutron matter constraints

H: Hebeler et al. (2010) and in prep.

G: Gandolfi et al. (2011)

predicts correlation  
but not range of  $S_v$  and  $L$





# Chiral Effective Field Theory for nuclear forces

Separation of scales: low momenta  $\frac{1}{\lambda} = Q \ll \Lambda_b$  breakdown scale  $\sim 500$  MeV

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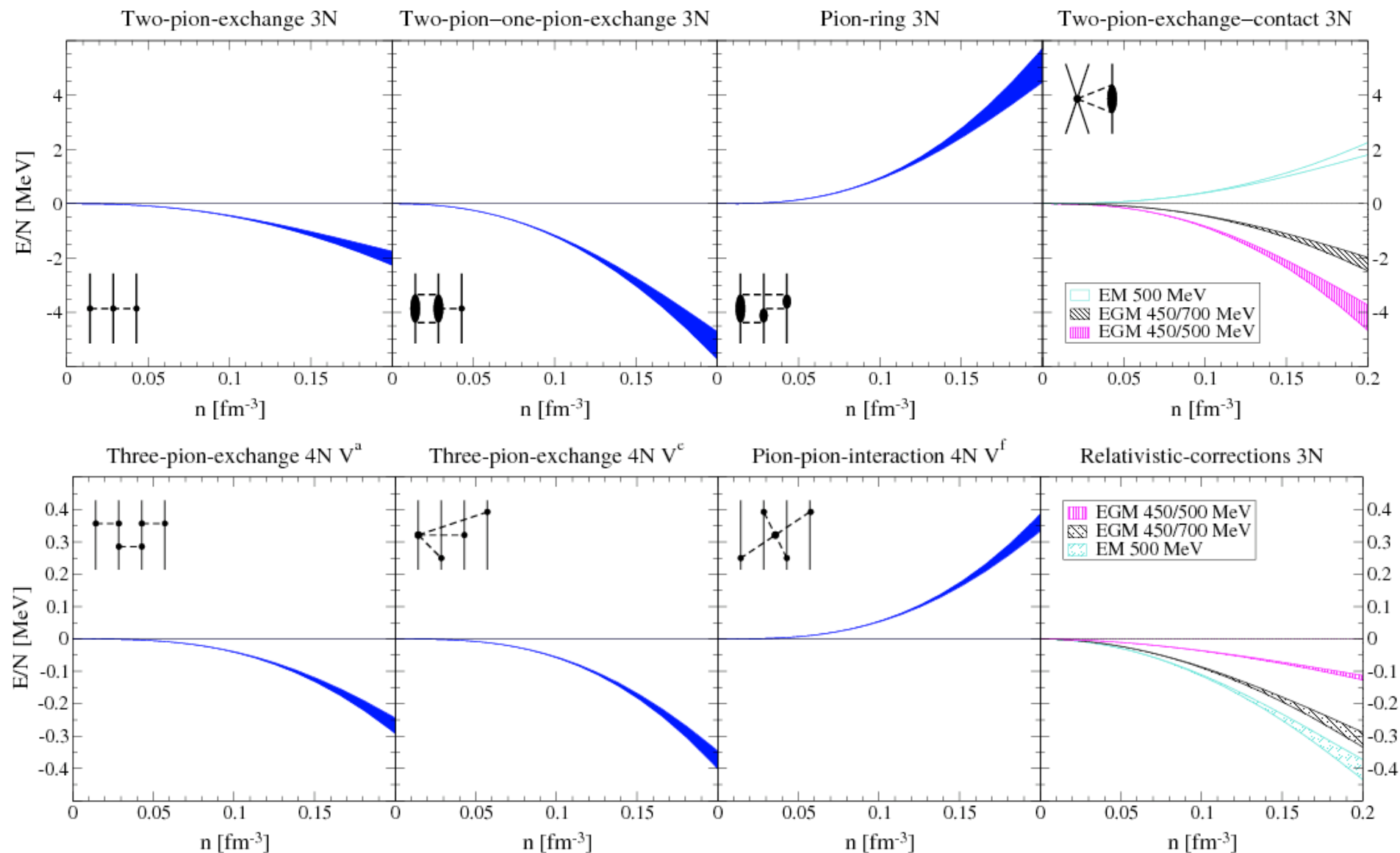
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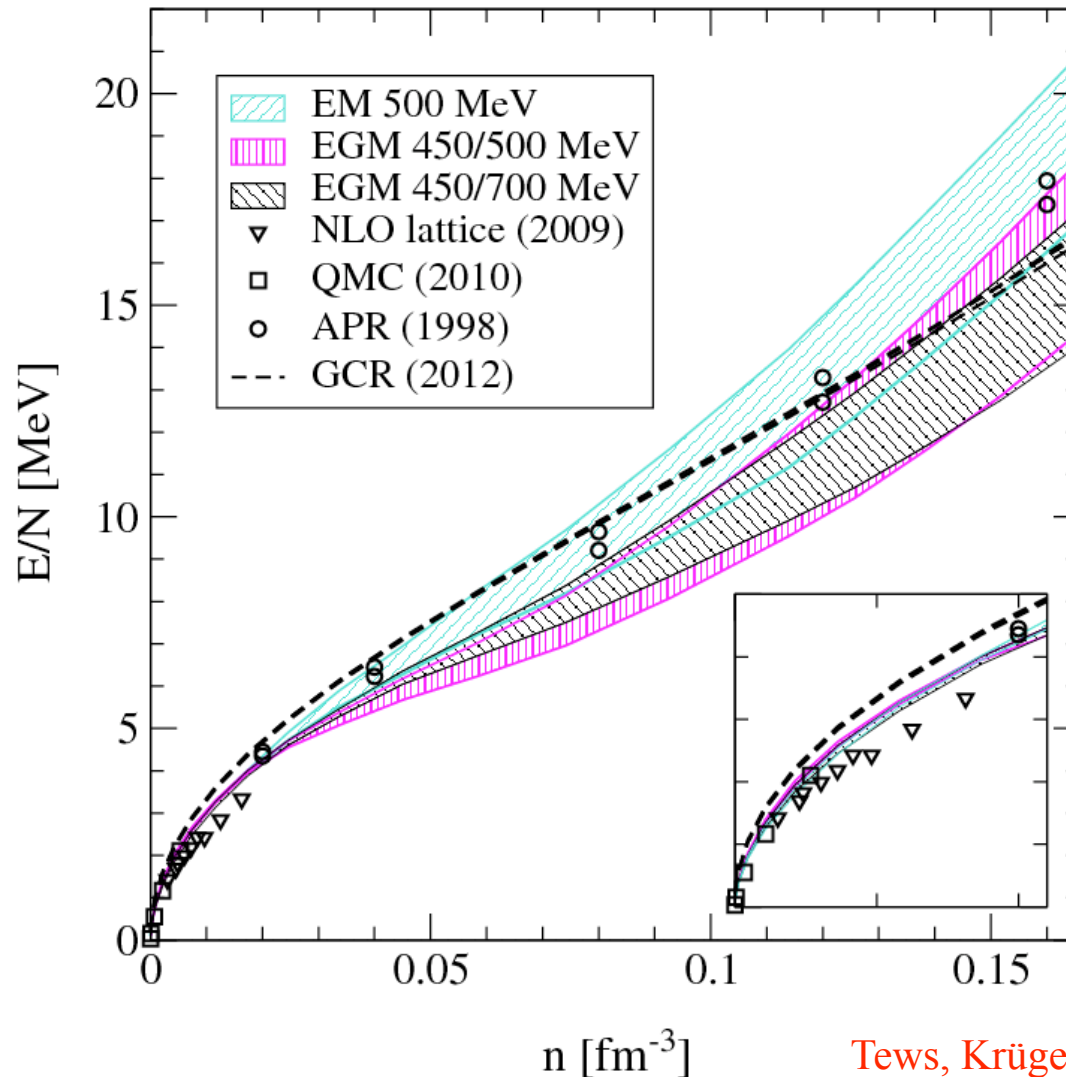
# Complete N<sup>3</sup>LO calculation of neutron matter



# Complete $N^3$ LO calculation of neutron matter

first complete  $N^3$ LO result

no RG evolution necessary, includes uncertainties from bare NN, 3N, 4N



**The Bertsch problem**



Tews, Krüger, Hebeler, AS, arXiv:1206.0025.

# Discovery of the heaviest neutron star

## A two-solar-mass neutron star measured using Shapiro delay

P. B. Demorest<sup>1</sup>, T. Pennucci<sup>2</sup>, S. M. Ransom<sup>1</sup>, M. S. E. Roberts<sup>3</sup> & J. W. T. Hessels<sup>4,5</sup>

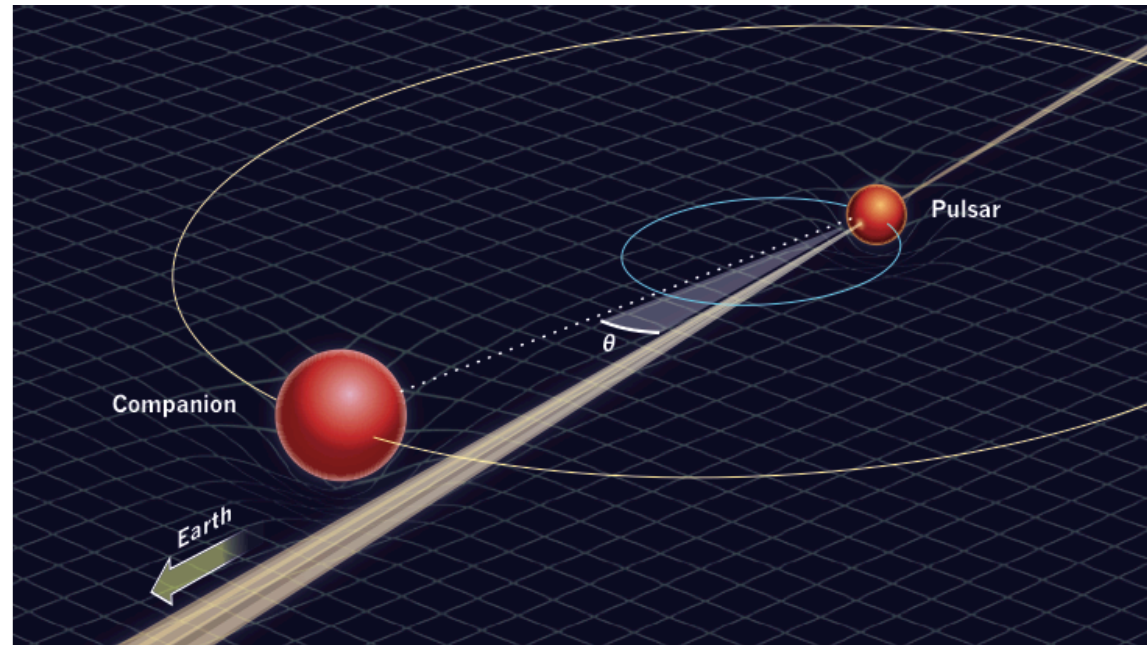
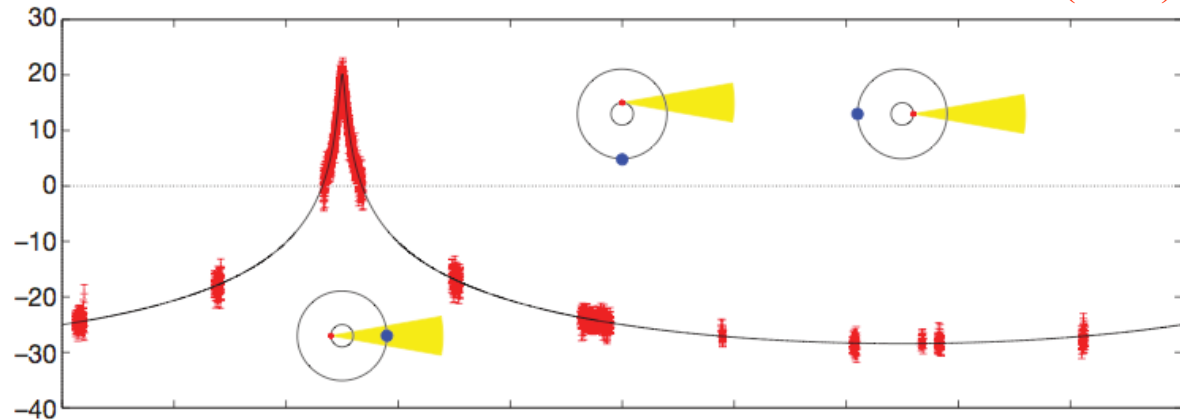
Nature (2010)

direct measurement of  
neutron star mass from  
increase in signal travel  
time near companion

J1614-2230

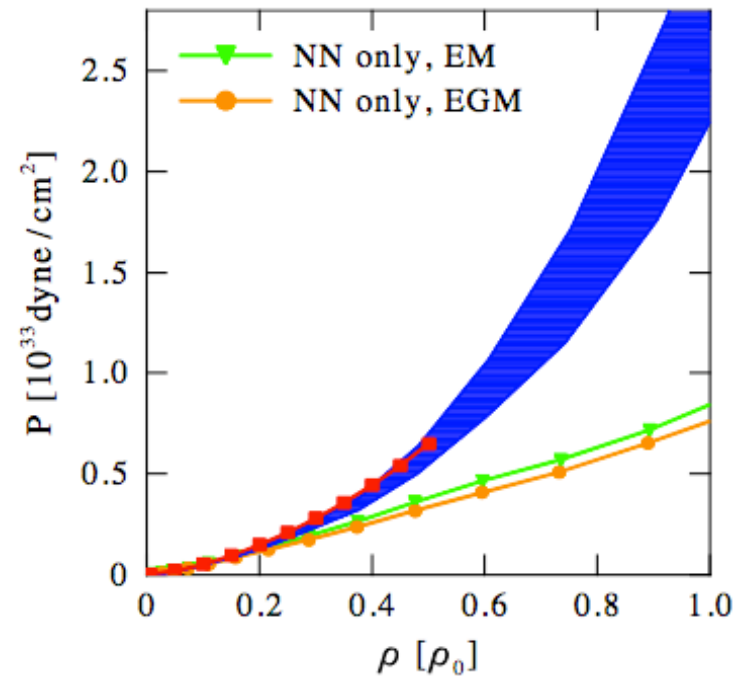
most edge-on binary  
pulsar known ( $89.17^\circ$ )  
+ massive white dwarf  
companion ( $0.5 M_{\text{sun}}$ )

heaviest neutron star  
with  $1.97 \pm 0.04 M_{\text{sun}}$



# Impact on neutron stars Hebel et al. (2010) and in prep.

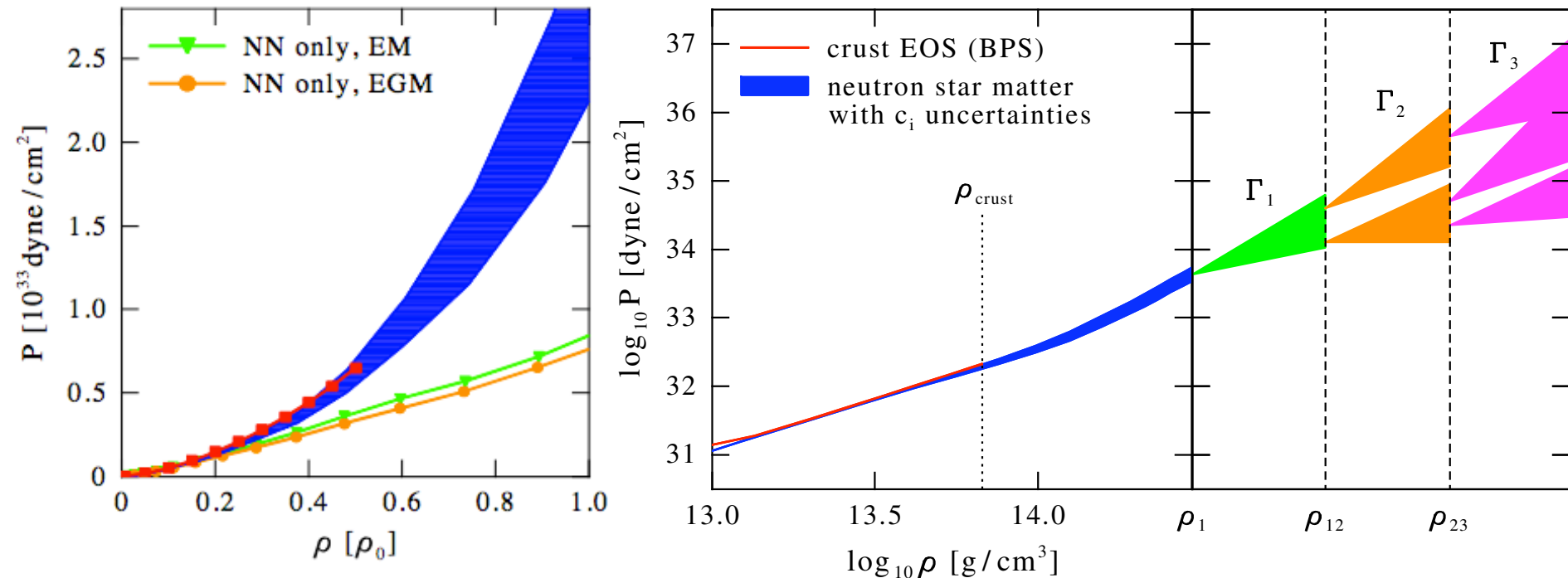
Equation of state/pressure for **neutron-star matter** (includes small  $Y_{e,p}$ )



pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

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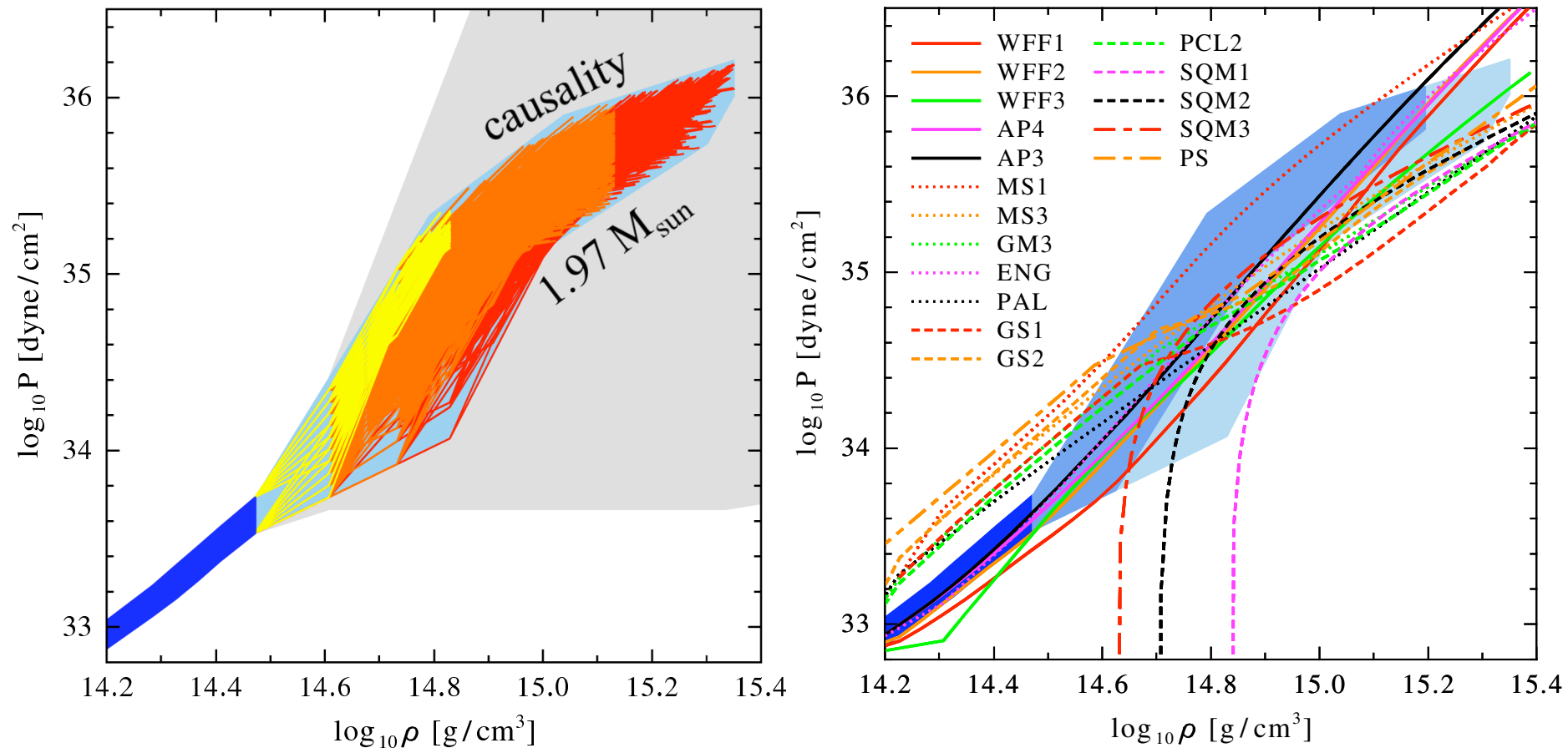
pressure below nuclear densities agrees with standard crust equation of state only after 3N forces are included

extend uncertainty band to higher densities using piecewise polytropes  
allow for soft regions



# Pressure of neutron star matter

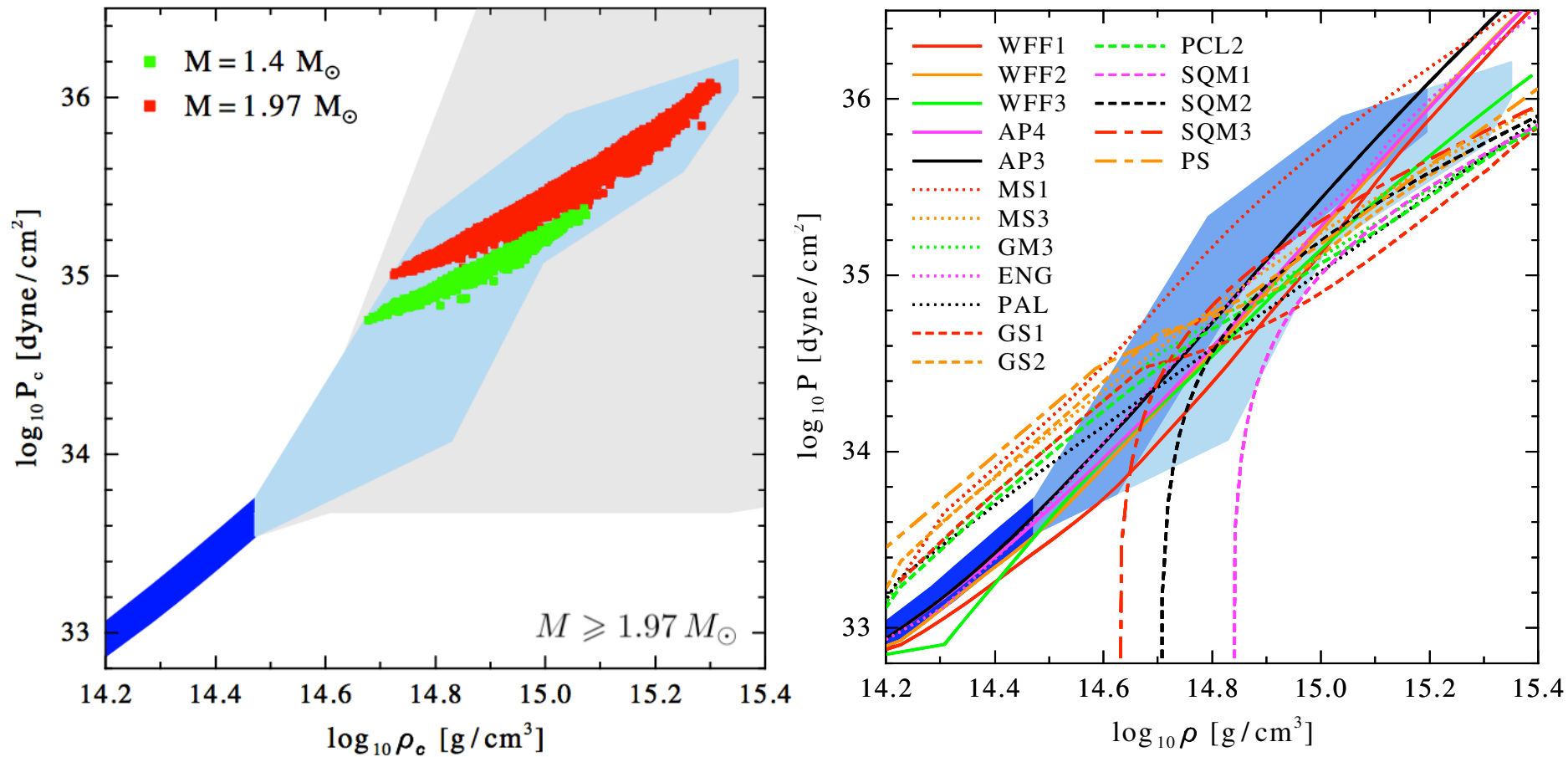
constrain polytropes by causality and require to support  $1.97 M_{\text{sun}}$  star



low-density pressure sets scale, chiral EFT interactions provide strong constraints, ruling out many model equations of state

# Pressure of neutron star matter

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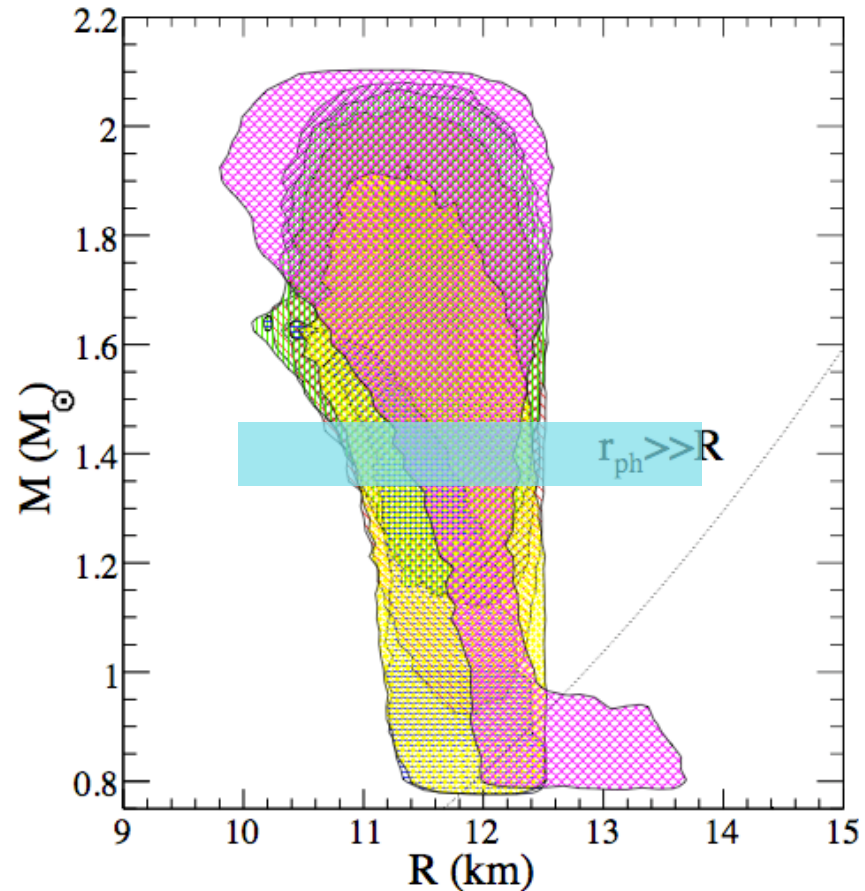
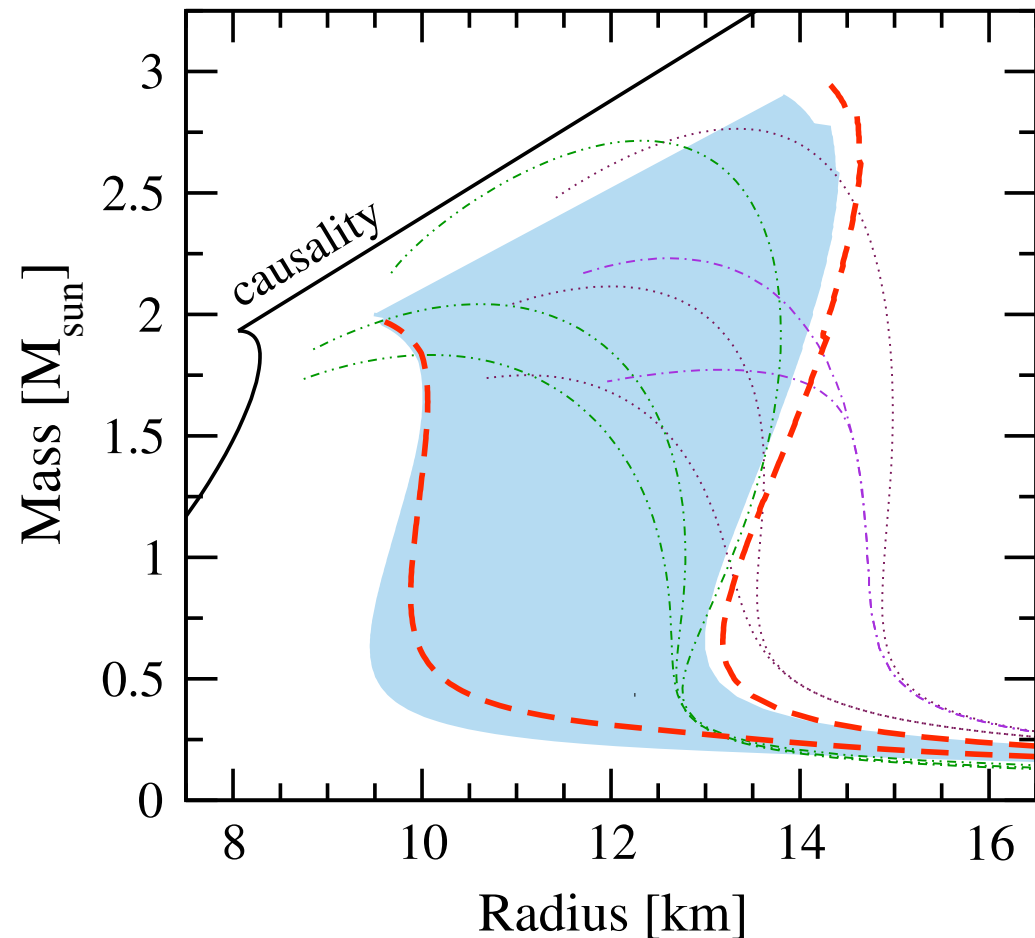


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**central densities for  $1.4 M_{\text{sun}}$  star:  $1.7\text{-}4.4 \rho_0$**

# Neutron star radius constraints

uncertainty from many-body forces and general extrapolation

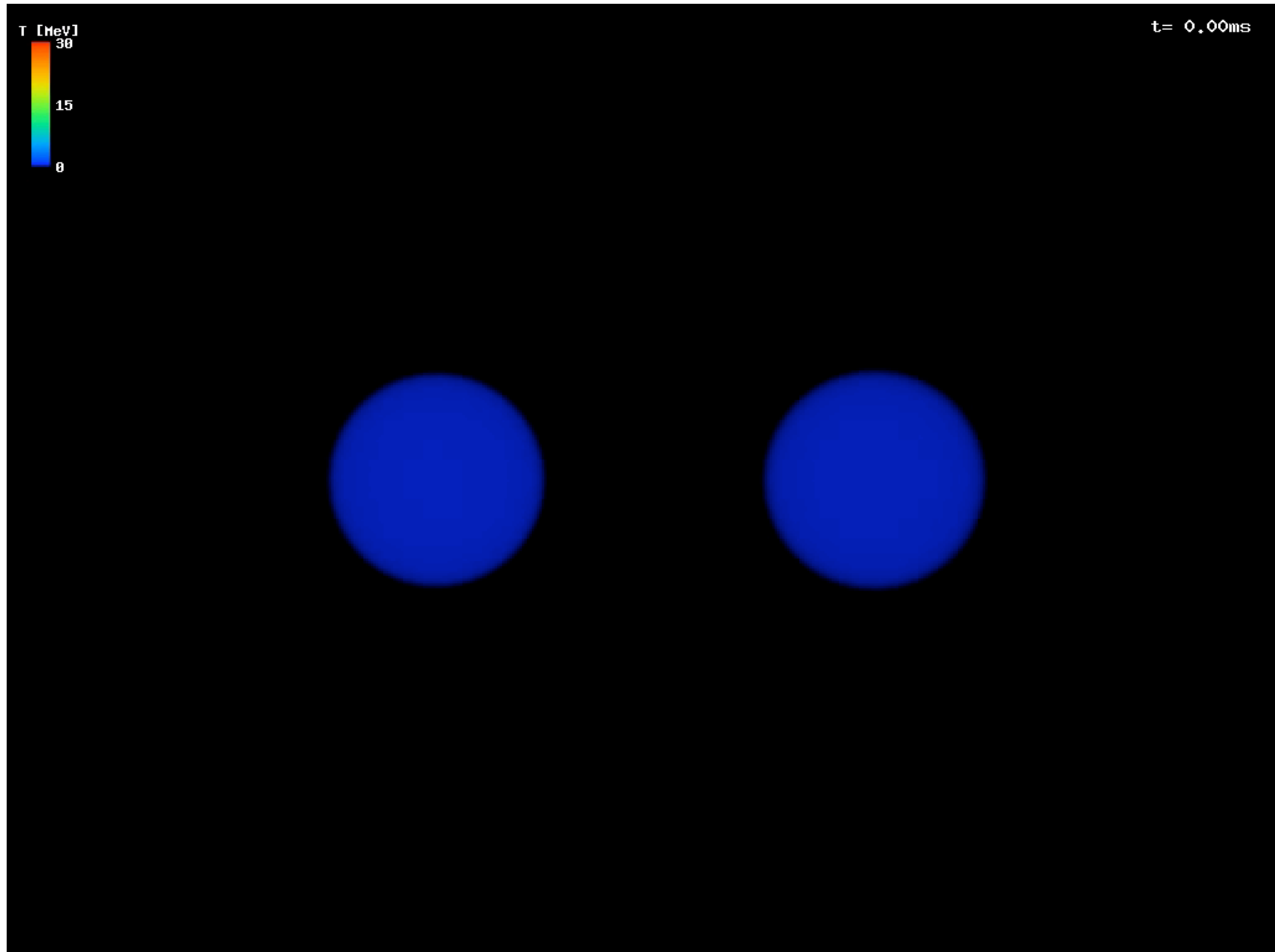


constrains neutron star radius: 9.9-13.8 km for  $M=1.4 M_{\text{sun}}$  ( $\pm 15\%$  !)

consistent with extraction from X-ray burst sources [Steiner et al. \(2010\)](#)

provides important constraints for EOS for core-collapse supernovae

# Neutron-star mergers and gravitational waves



# Neutron-star mergers and gravitational waves

explore sensitivity to neutron-rich matter in neutron-star merger and gw signal

Bauswein, Janka (2012) and A. Bauswein et al., arXiv:1204.1888.

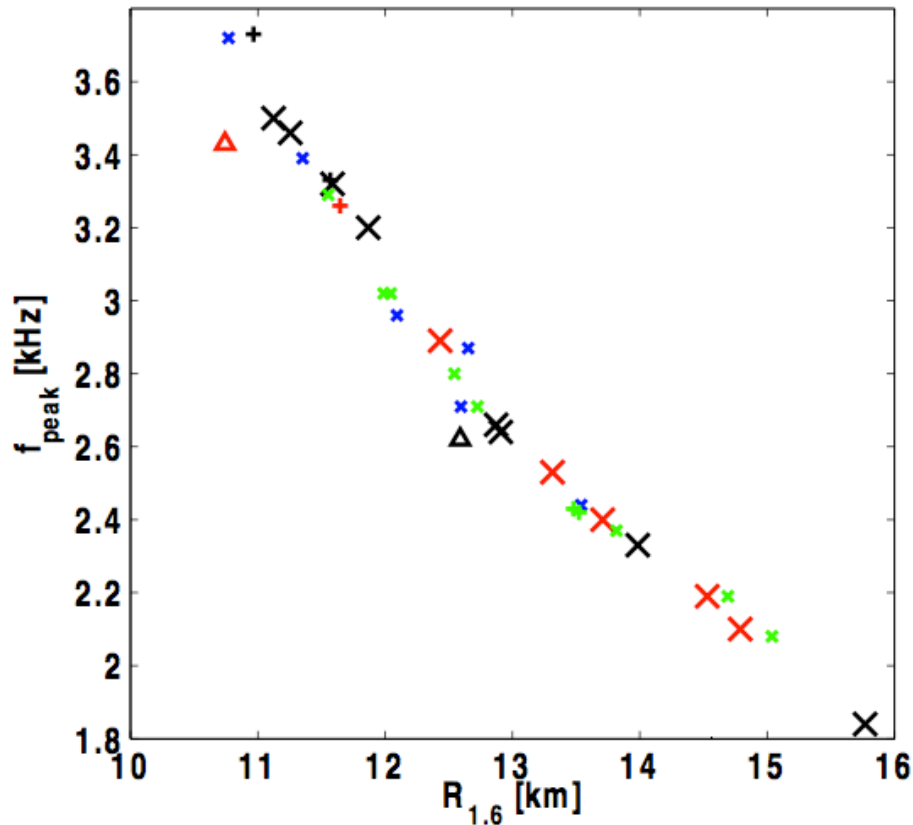
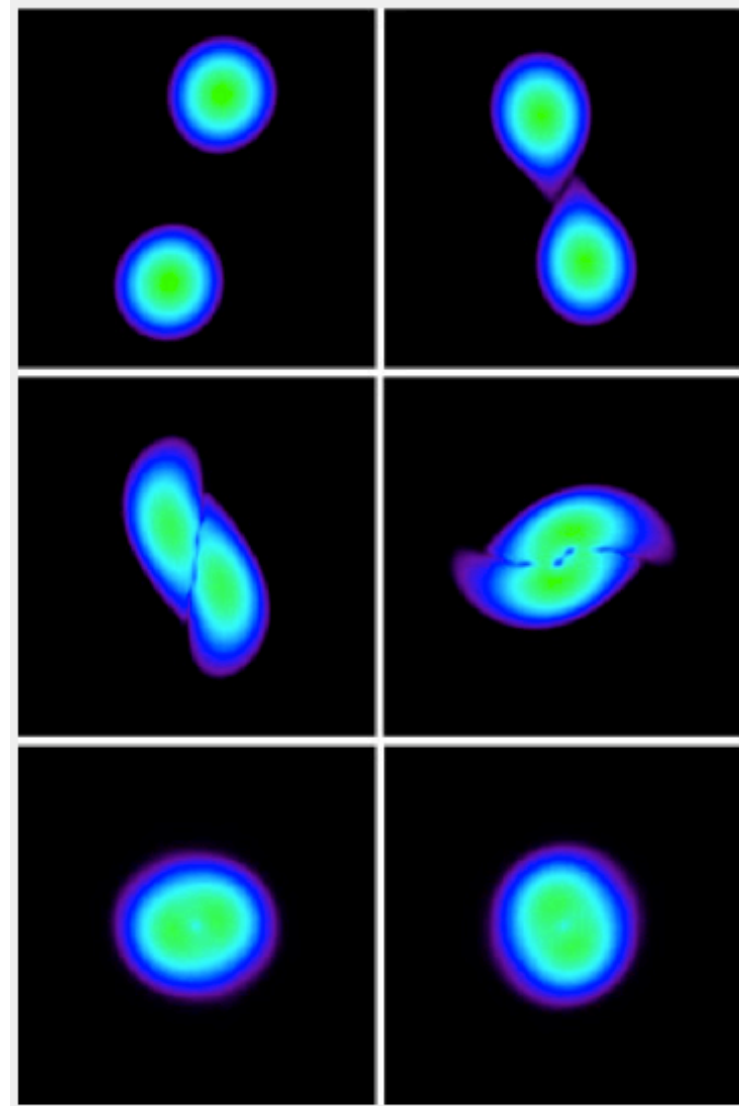


FIG. 10: Peak frequency of the postmerger GW emission versus the radius of a nonrotating NS with  $1.6 M_{\odot}$  for different EoSs. Symbols have the same meaning as in Fig. 8.



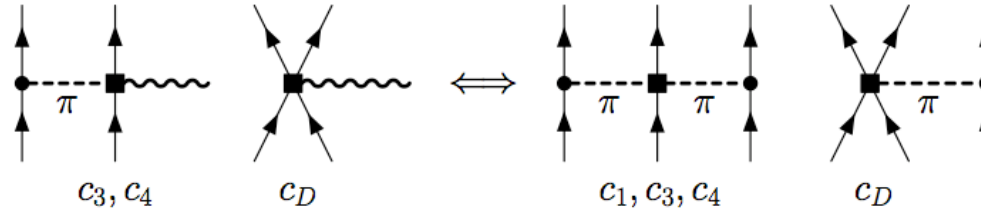
**Fig. 1:** Various snapshots of the collision of two neutron stars initially revolving around each other. The sequence simulated by the computer covers only 0.03 seconds. The two stars orbit each other counterclockwise (top left) and quickly come closer (top right). Finally they collide (centre left), merge (centre right), and form a dense, superheavy neutron star (bottom). Strong vibrations of the collision remnant are noticeable as deformations in east-west direction and in north-south direction (bottom panels). (Simulation: Andreas Bauswein and H.-Thomas Janka/MPA)

# Electroweak interactions and 3N forces

weak axial currents couple to spin, similar to pions

two-body currents predicted by NN, 3N couplings to  $N^3LO$

Park et al., Phillips,...



two-body analogue of Goldberger-Treiman relation

explored in light nuclei (reactions for SNO), but not for larger systems

dominant contribution to Gamow-Teller transitions,  
important in nuclei ( $Q \sim 100$  MeV)

3N couplings predict quenching of  $g_A$  (dominated by long-range part)  
and predict momentum dependence (weaker quenching for larger  $p$ )

Menendez, Gazit, AS (2011)

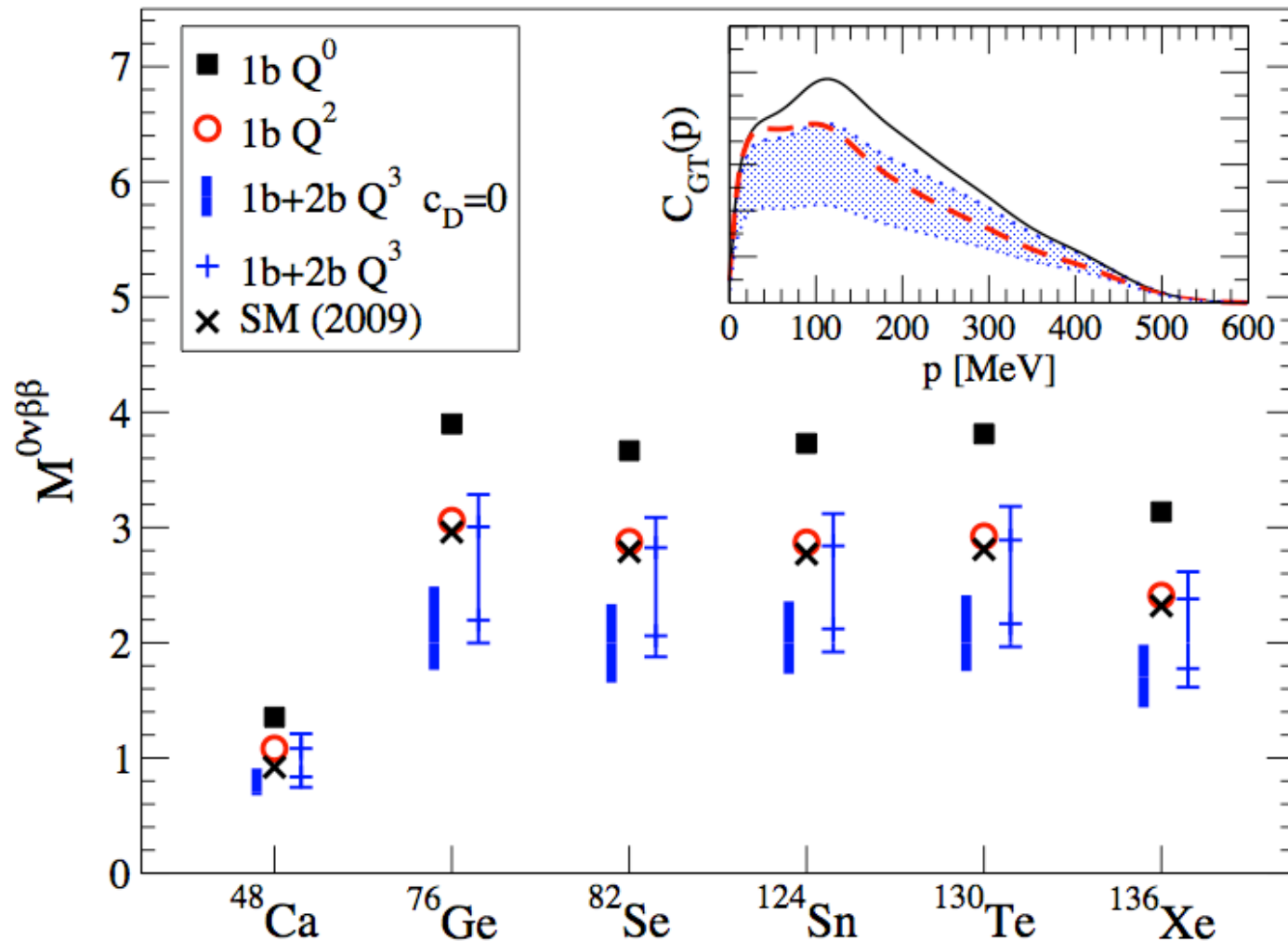


# Chiral EFT and $0\nu\beta\beta$ decay

Nuclear matrix elements for  $0\nu\beta\beta$  decay based on chiral EFT operator

Menendez, Gazit, AS (2011)

Modest quenching because  $0\nu\beta\beta$  decay probes higher momentum transfer



## Summary

3N forces are a frontier for neutron-rich nuclei, matter, neutron stars:

key to explain why  $^{24}\text{O}$  is the heaviest oxygen isotope

key for neutron-rich nuclei: Ca isotopes,  $N=28$  and shell evolution

dominant uncertainty of neutron (star) matter below nuclear densities

predicts neutron skin with theoretical uncertainty comparable to exp.

constrains neutron star radii and equation of state for astrophysics

impact of 3N forces on global mass predictions?

exciting interactions with George, experiments and observations!